Article

Area per Lipid and Cholesterol Interactions in Membranes from Separated Local-Field $^{13}$C NMR Spectroscopy

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ABSTRACT Investigations of lipid membranes using NMR spectroscopy generally require isotopic labeling, often precluding structural studies of complex lipid systems. Solid-state $^{13}$C magic-angle spinning NMR spectroscopy at natural isotopic abundance gives site-specific structural information that can aid in the characterization of complex biomembranes. Using the separated local-field experiment DROSS, we resolved $^{13}$C-$^1$H residual dipolar couplings that were interpreted with a statistical mean-torque model. Liquid-disordered and liquid-ordered phases were characterized according to membrane thickness and average cross-sectional area per lipid. Knowledge of such structural parameters is vital for molecular dynamics simulations, and provides information about the balance of forces in membrane lipid bilayers. Experiments were conducted with both phosphatidylcholine (dimyristoylphosphatidylcholine (DMPC) and palmitoyloleoylphosphatidylcholine (POPC)) and egg-yolk sphingomyelin (EYSM), and allowed us to extract segmental order parameters from the $^{13}$C-$^1$H residual dipolar couplings. Order parameters were used to calculate membrane structural quantities, including the area per lipid and bilayer thickness. Relative to POPC, EYSM is more ordered in the $l_d$ phase and experiences less structural perturbation upon adding 50% cholesterol to form the $l_p$ phase. The loss of configurational entropy is smaller for EYSM than for POPC, thus favoring its interaction with cholesterol in raftlike lipid systems. Our studies show that solid-state $^{13}$C NMR spectroscopy is applicable to investigations of complex lipids and makes it possible to obtain structural parameters for biomembrane systems where isotope labeling may be prohibitive.

INTRODUCTION

Lipid-protein interactions (1) and the associated functions of biomembranes (2–6) are known to be significantly influenced by the composition (2,7–11) and structure of the lipid bilayer (6,11–16). Recently, the importance of lipids in cellular membranes and tissues has made lipidomics (17) an emerging field in biomedical research. Essential roles of membrane lipids are brought out by the sphingolipids, which are implicated in human disorders including Tay-Sachs, Niemann-Pick, Gaucher (18), Parkinson’s (19), and Huntington diseases (20). Sphingolipids are attracting much attention to so-called lipid rafts in cellular membranes (4,9,21–27). Moreover, in vitro studies of integral membrane proteins or peptides often require that they be reconstituted with membrane lipids (19,28–30), where bilayer structural dimensions involving hydrophobic matching and area per lipid are significant factors (1,14,31). The constraints imposed by the area per lipid at the membrane aqueous interface (31) also play an important part in validating molecular dynamics (MD) simulations of lipid bilayers (32) and biomembranes (13,33,34). In such cases, it is essential that investigators have a solid understanding of the membrane bilayer structure itself (35).

Despite advances in technology (19,36–45), there is an enduring thirst for new methods on account of the strengths and limitations inherent in existing biophysical techniques. This work is aimed at extending such investigations by using for the first time to our knowledge a combination of separated local-field (SLF) NMR spectroscopy (41,46–48) and statistical mean-torque theory (35). Studies of natural lipids, as well as natural detergents (49), can benefit from extending methods originally developed for $^2$H NMR spectroscopy (50) to cases where $^2$H-isotope labeling is impractical. Simple geometrical observations are the basis of a mean-field model used for analysis of both small-angle x-ray scattering (SAXS) and solid-state $^2$H NMR data (51). The first-order mean-torque model (35) evaluates the average cross-sectional area and volumetric hydrocarbon thickness of the membrane lipids. For multicomponent membranes, the ensemble structures derived from the repeat spacings or electron densities in SAXS do not resolve the contributions from individual lipid species. However, average cross-sectional areas for multicomponent lipid mixtures are obtainable from residual quadrupolar couplings in solid-state $^2$H NMR spectroscopy, which typically requires isotopically labeled lipids for each component studied (52).

Here, we demonstrate the applicability of mean-field modeling of membrane structure in conjunction with a solid-state $^{13}$C NMR technique that does not require isotopic enrichment. Magic-angle spinning (MAS) NMR resolves site-specific details for individual lipid species in...
membranes (28,47,53–56), thus enabling a range of biologically significant applications. We show how the steric hydrocarbon thickness and average cross-sectional areas are derived from solid-state $^{13}$C-$^1$H residual dipolar couplings (RDCs) for sphingolipids and phospholipids in single-component and cholesterol-enriched binary mixtures. Two-dimensional (2D) solid-state $^{13}$C NMR spectroscopy (46) can probe the headgroup, backbone, and acyl chain regions for membrane components simultaneously, including cholesterol at natural isotopic abundance (19,46,57). In addition, the membrane phase behavior is further quantified, giving a valuable probe of lipid interactions in bilayers, as well as in natural biomembranes.

MATERIALS AND METHODS

Preparation of multilamellar lipid dispersions

1,2-dimyristoyl-sn-glycero-3-phosphocholine (DMPC), 1-palmitoyl-2-oleyl-sn-glycero-3-phosphocholine (POPC), and egg yolk sphingomyelin (EYSIM) (predominant species N-(palmitoyl)-sphing-4-enine-1-phosphocholine) were procured from Avanti Polar Lipids (Alabaster, AL), and cholesterol (cholesterol) was from Sigma-Aldrich (St. Louis, MO). The lipids were dissolved in hexane and lyophilized to yield dry powders. Multilamellar lipid dispersions were prepared by hydrating the dry lipid powders with 50 wt% deuterium oxide (Cambridge Isotopes, Cambridge, MA). These lipid dispersions were prepared in 4-mm zirconium rotors. Radiofrequency pulses for the $^1$H dipolar coupling on-axis with scaling and shape preservation (DROSS) (46) was implemented on the Bruker Topspin 2.1 software platform (Billerica, MA). A triple-channel MAS NMR probe (DSI-733) from Doty Scientific (Columbia, SC) was used for all experiments. Samples were contained in 4-mm zirconium rotors. Radiofrequency pulses for the $^1$H and $^{13}$C channels were adjusted to exactly the same duration, 3.5 $\mu$s for the 90° pulses. Dipolar recoupling at 6–8 kHz MAS frequency was achieved by applying four radiofrequency 180° pulses in one rotor period, with a chemical shift offset of $e=0$ and anisotropy scaling of $c_h=0.393$ (46,58). The INEPT (insensitive nuclei enhanced by polarization transfer) buildup of anti-phase magnetization and refocusing delays was optimized empirically. The rotor-synchronized sampling of the indirect dimension ($t_2$) was achieved using the States method with a total of 64–128 points. The sampling of the direct time dimension ($t_1$) utilized 8192 points recorded with an interval of 10 ms with 50-kHz $^1$H SPINAL-32 decoupling (59). Recycle times were 3 s, and between 1000 and 2000 transients were averaged for each $t_2$ record, giving total experiment times ranging from 24–48 h. The fluctuations in rotor spinning speed were controlled to $\pm 2$ Hz with a Doty Scientific spin-rate controller. Sample temperature was controlled using a Bruker variable temperature unit and is accurate to $\pm 1^\circ$C. The reported $^{13}$C NMR chemical shifts were referenced to TMS (external).

Fourier transformation of the $t_1$ and $t_2$ dimensions was carried out and analyzed using the Bruker Topspin software. A 10-Hz Lorentzian broadening was applied in the $t_2$ dimension, and a 50- to 250-Hz Gaussian apodization was applied in the $t_1$ dimension after zero-filling to 128–256 points.

Fits to $^{13}$C SLF DROSS magnetic dipolar lineshapes were generated using the Topspin solid lineshape analysis (SOLA) software and verified using standard algorithms for the Pake lineshape coded in Matlab (Natick, MA). Segmental order parameters are defined as (50)

$$S_{CH} = \frac{1}{2} \left( 3 \cos^2 \beta_{CH} - 1 \right),$$

where $\beta_{CH}$ is the instantaneous angle between the $^{13}$C-$^1$H bond direction and the bilayer normal. Based on geometrical considerations, the $S_{CH}$ order parameters for a polymethylene chain are negative.

Here we refer to the absolute order parameters $|S_{CH}|$, calculated from the relation

$$|S_{CH}| = \frac{|\Delta\nu_{DP}|}{\nu_P \nu_P}$$

In the above formula, $\chi_3 = (-\mu_0 H/4\pi)^2 r^{-3}$ is the dipolar coupling constant (40,783 kHz corresponding to $b_{CH}2\pi = 20,392$ kHz) for an aliphatic $^{13}$C-$^1$H bond (46). $\chi_3 = 0.393$ is the pulse-sequence scaling factor (46), and $\Delta\nu_{DP}$ is the measured RDC evaluated at the $\theta = 90^\circ$ orientation of the lineshape (Pake powder pattern). The estimated random error of the RDCs is $\pm 4\%$, corresponding to a $\pm 4\%$ error of the segmental order parameters. Possible sources of systematic errors include the value of the rigid-lattice (static) dipolar coupling constant as well as the chemical-shift assignments. Note that the above dipolar coupling constant corresponds to an effective equilibrium internuclear $^{13}$C-$^1$H distance of $r^{-3}$ due to the correction for dynamic effects, as first shown in our previous work (69). For resonance assignments of the $^{13}$C isotopic chemical-shift spectra, ChemBioDraw (PerkinElmer, Waltham, MA)-based simulations based on additivity relations for isotropic lipids (61–65) were initially used. However, because the chemical shifts due to liquid-crystalline phase conformations are not averaged to their isotropic values, we introduced $^2$H NMR-derived $|S_{CD}|$ order-parameter-based peak assignments (43). In this article, we compare the calculated $|S_{CH}|$ order parameter values with $|S_{CD}|$ order parameters used for the peak assignments. Such methods are helpful in identifying the $^{13}$C resonance peaks coming from the hydrocarbon chains of the liquid-crystalline phospholipids.

Theoretical Framework of Mean-Torque Model

For membrane lipids, the dipolar or quadrupolar couplings are reduced from their rigid-lattice (static) values due to segmental and molecular motions as well as collective fluctuations of the entire bilayer (66). The various motions are described by their mean-squared amplitudes and (reduced) spectral densities, and they may include cross correlations due to their statistical (in) dependence (66–68). The segmental order parameters ($S_{CH}$ or $S_{CD}$) describe the collective motion in terms of the residual couplings (dipolar or quadrupolar) as compared to the static values (43). The order parameters are model-free spectroscopic observables that are statistical averages over all the motions, with correlation times up to the inverse of the rigid-lattice coupling (50). In analogy with liquid crystals, each segment is considered independently, because the spectroscopic observables are site-specific (50,69). Correlations among the motions along the chains and between the chains are included in the order parameters as a function of segmental position (35,70). Interpretation of the segmental order parameters in terms of lipid bilayer structure was first achieved using a diamond-lattice model (71,72). That model assumes discrete orientations of acyl chain segments as the most probable conformations. Although initially it appeared to be reasonably good agreement with scattering experiments, discrepancies between the area calculations from more accurate $^2$H NMR and x-ray scattering measurements became evident (73,74). The mean-torque model was proposed as an alternative (35), as it assumes a continuum distribution for the orientations of acyl chain segments. The mean-torque model successfully explains bilayer structural parameters for liquid-crystalline disaturated phospholipid membranes (35).
In this work, we introduce the applicability of the mean-torque model in connection with $^{13}$C-NMR-derived segmental order parameters to interpret the membrane structure. Here, the main objective is connecting the lipid structural parameters to hydrocarbon-chain segmental order parameters. Changes due to osmotic stress or to headgroup and acyl chain composition are related to the balance of forces that govern membrane assembly and lipid-protein interactions (1). For disaturated lipids, a plateau is seen in the $^2$H-NMR-derived segmental order parameter profile close to the headgroup. At a certain depth of the bilayer, the influence of chain terminations becomes important (75,76). Acyl chains on adjacent molecules become more disordered beyond this point to maintain the packing of hydrocarbon density (77). Another observation from $^2$H NMR order profiles is that the plateau region shows a strong chain-length dependence, whereas nonplateau regions are practically independent of chain length (35). At the molecular scale, each lipid in the membrane occupies a space that on average is related to the volume and length of the hydrocarbon chains according to

$$D_C = \frac{2V_C}{\langle A \rangle}, \quad (3)$$

where $D_C$ is the volumetric thickness of the hydrocarbon layer, and $V_C$ is the total volume of an individual acyl chain. In Eq. 3, the volume, $V_C$, is assumed from the densitometry measurements of Nagle and co-workers (78) and is conserved (i.e., constant). Note that the volumetric thickness, $D_C$, and the mean area, $\langle A \rangle$, are inversely related by the assumption of constant volume, meaning that the bilayer core has approximately the density of liquid hydrocarbon (77,80). However, $D_C$ is not the same as the mean projected acyl length, as discussed by Jansson et al. (79). Due to end effects of the acyl chains, the mean travel away from the aqueous interface is less than the distance to the bilayer midplane, as required for the well-established assumption of constant volume to apply (35). The chain volume at temperature $T$ is found from the methylene volume, $V_{CH_2}$, using the expression $V_{CH_2} = V_0^{CH_2} + \alpha_{CH_2} (T - 273.15)$, where $\alpha_{CH_2}$ is the isobaric thermal expansion coefficient for methylene groups (35). It is well established that the volume of a methyl group is $V_{CH_3} = 2V_{CH_2}$, and that $V_{CH_2} = V_{CH_2}/1.31$ for the methyne volume (78,80,81).

When the membrane composition is mixed, neighboring interactions between the lipids can lead to a change in the average cross-sectional area per lipid. To avoid complications from chain upturns (35,70), for estimating the average area per lipid instead of the area of the entire hydrocarbon chain, the mean area per lipid is thus given as (35)

$$\langle A \rangle = 4V_{CH_2} \left( \frac{1}{D} \right). \quad (4)$$

Here $V_{CH_2}$ is the methylene volume (78) and $D$ is the instantaneous travel of an individual segment along the bilayer normal. This expression can be further rewritten as

$$\langle A \rangle = \frac{4V_{CH_2}}{D_M} q, \quad (5)$$

where $D_M = 2.54$ Å is the maximum projection of the virtual bonds connecting every second carbon atom in the polymethylene chain to the bilayer normal, and $4V_{CH_2}/D_M$ is the lipid cross-sectional area of the extended all-trans conformation (35). The area factor $q$ is defined as $\langle 1/\cos \beta \rangle^{-1}$, where $\beta$ is the angle between the virtual bond axis connecting the $C_{i-2}$ and $C_{i+1}$ carbon atoms and the normal to the lipid bilayer surface.

In Eq. 5, Euclidean geometry is assumed by approximating the shape of a statistical segment by a geometrical prism with constant hydrocarbon volume (50). Consequently, the effective acyl segment length is averaged over the motions, whereas the segmental volume is not. As the motional amplitudes increase, so does the area per lipid, yet the volume per segment spanned in space remains approximately constant. It follows that a Taylor series expansion about the all-trans reference value allows the area factor $q$ to be approximated by $q \approx 3 - 3(\cos \beta_i) + (\cos^2 \beta_i)$ up to second order (35). For $^{13}$C NMR, the second moment $\langle \cos^2 \beta_i \rangle$ can be obtained directly from the absolute order parameters $S_{CH}^{(i)}$ of a given acyl segment (index $i$) by

$$\langle \cos^2 \beta_i \rangle = \frac{1 + 4|S_{CH}^{(i)}|}{3} \quad (6)$$

To interpret the $S_{CH}^{(i)}$ dipolar order parameters in terms of structural quantities, several models have been developed (35). Because of the inherent complexity of membrane structure, most of these models are confined to simplified statistical treatments of lipid conformations. Calculation of the first moment $\langle \cos \beta_i \rangle$ with a given value of $\langle \cos^2 \beta_i \rangle$ is further described below.

The mean-torque model assumes that the orientational order for each chain segment relative to the local director is described by an orientational potential, $U(\beta)$ (potential of mean torque). With the combined effects of thermal fluctuations of the segmental orientations, both segmental and molecular conformations assume a continuous distribution. The probability of finding a statistical segment with a virtual bond orientation $\beta (\equiv \beta_{CH_2})$ at a given instant is given by the Boltzmann distribution,

$$f(\beta) = \frac{1}{Z} \exp \left( - \frac{U(\beta)}{k_b T} \right), \quad (7)$$

where the chain index $i$ is also suppressed for clarity. Here, the partition function is

$$Z = \int_0^\pi \exp \left( - \frac{U(\beta)}{k_b T} \right) \sin \beta d\beta. \quad (8)$$

Assuming a first-order mean-torque model (35), the angle-dependent quantities are integrated with the distribution function to give the coupled equations

$$\langle \cos \beta \rangle = \frac{U(\beta)}{k_b T} + \left( \frac{U(\beta)}{k_b T} \right)^{-1}; \quad (9)$$

$$\langle \cos^2 \beta \rangle = 1 + 2 \left( \frac{U(\beta)}{k_b T} \right)^{-2} - 2 \left( \frac{U(\beta)}{k_b T} \right)^{-1} \coth \left( \frac{U(\beta)}{k_b T} \right). \quad (10)$$

An analytical solution for $\langle \cos \beta \rangle$ can then be obtained by using the approximation $\coth(U/2k_b T) \approx 1$, which for an individual segment (index $i$) yields the relation

$$\langle \cos \beta_i \rangle = \frac{1}{2} \left( 1 + \sqrt{\frac{8|S_{CH}^{(i)}| - 1}{3}} \right). \quad (11)$$

It should be noted that for the all-trans conformation of the lipids, $\langle \cos \beta_i \rangle = \langle \cos^2 \beta_i \rangle = 1$ and hence $q = 1$. It follows that Eqs. 3 and 4 give rise to a limiting area of $4V_{CH_2}/D_M$ and limiting monolayer thickness of $n_cD_M/2$, where $n_c$ is the number of carbon atoms in the hydrocarbon chain.

Each molecule contributes to the average thickness for the lipid bilayer ensemble, which includes the headgroup plus backbone thickness in the sense of a Gibbs dividing surface. The volumetric (Luzzati) bilayer...
thickness is $D_b = V_i / (\lambda)$ where $V_i$ is the lipid volume (78) and $D_H = 4 \, \text{Å}$ for DMPC or POPC and 6 Å for EYSM. Alternatively, an effective membrane bilayer thickness can be calculated using the expression,

$$D_b' = 2D_C + 2D_H,$$

(12)

where $D_C$ is the volumetric hydrocarbon thickness of the two acyl chains of the lipid, and $D_H$ is the headgroup plus the backbone distance. In the case of phospholipids, $D_H$ is 9 Å, and for most sphingolipids it is 7 Å (82–84). Use of the above values of $D_H$ and $D_C$ corresponds to the steric bilayer thickness $D_b'$ as defined by Nagle et al. (12). Finally, it is important to note that the first-order mean-torque model neglects the effects of collective slow motions (77). The above treatment of a mean-torque model was originally formulated in terms of $^2$H NMR-derived $S_{CD}$ values. However, we show equivalently that one can use $S_{CH}$ order parameters obtained from natural-abundance $^{13}$C NMR spectroscopy to extend the calculation of membrane structural parameters.

**RESULTS**

The INEPT-based SLF NMR experiment DROSS (46) was implemented for the two glycerophospholipids DMPC and POPC together with the sphingolipid EYSM and their binary mixtures with cholesterol. The DROSS experiment provides measurements for the headgroup, glycerol backbone, and acyl chain order parameters without isotopic enrichment. This is especially useful when comparing responses from these bilayer regions to changes in bilayer composition. However, accurate measurement of small absolute order parameters, as in the case of headgroup segments (85), is challenging in SLF spectroscopy. As an example, Fig. 1 shows a 2D SLF spectrum of a POPC/cholesterol (1:1) binary mixture at 30°C. The representative slices of the 2D DROSS spectrum shown in Fig. 1 a indicate that well-resolved RDCs (Pake doublets) are obtained. The RDCs can be used to obtain dipolar $^{13}$C–$^2$H order parameters that are analogous to the C–$^2$H bond order parameters in solid-state $^2$H NMR spectroscopy (50). An expansion of the 2D DROSS spectrum from the aliphatic fingerprint region is shown in Fig. 1 b. The slices parallel to the $F_1$ frequency axis for each of the chemically shifted ($\delta$) resonances in the $F_2$ dimension give the site-specific RDCs (Pake doublets). Fig. 1 c shows a contour plot of the 2D DROSS spectrum together with the $F_2$ frequency projection corresponding to the 1D chemical-shift spectrum. A number of distinct $^{13}$C resonances are observed due to the POPC acyl groups as well as cholesterol. Notably, the (CH$_2$)$_n$ envelope includes additional acyl chain resonances that are incompletely resolved due to inhomogeneous line broadening. They can be partially assigned by comparison to the results of solid-state $^2$H NMR spectroscopy (see below). Further explanation of the SLF experiment is provided in Figs. S1–S4 in the Supporting Material.

**Liquid-disordered phase of lipid bilayers**

Our findings illustrate that SLF NMR spectroscopy is broadly applicable to a variety of synthetic and natural lipids. Fig. 2 a depicts a 2D plane of a DROSS spectrum for POPC in the liquid-crystalline state at 28°C. The $F_2$ frequency dimension (horizontal) shows the isotropic $^{13}$C chemical shift ($\delta$) spectra obtained under MAS. As mentioned above, the DROSS spectra contain Pake doublets corresponding to the $^{13}$C–$^2$H dipolar couplings along the $F_1$ frequency axis (vertical). The dipolar slices correspond to each of the isotropic $^{13}$C chemical-shift positions. A similar set of spectra representing EYSM at 48°C is shown in Fig. 2 b. Resonances from polar headgroups, glycerol backbone, and acyl chains of the lipids are clearly resolved. The $^{13}$C chemical-shift assignments were taken from the literature (86,87) and were verified by simulations based on additivity.
rules reported for isotropic liquids (61,62,64,65). Even so, in the spectral region between 29.5 ppm and 31.5 ppm there is considerable overlap of the resonances from lipid hydrocarbon chain segments.

Because literature chemical shifts are unavailable for individual carbons in this spectral region, initially we assigned those resonance peaks solely depending on 13C chemical shifts of isotropic liquids. For each of the resolved peaks, the spectra obtained for the F1 dimension were fit with Pake lineshapes to extract site-specific RDC values along the hydrocarbon chains, as well as for the lipid backbone and choline headgroup regions. The 1H-13C order parameter values were calculated according to Eq. 2. Results for the calculated \( S_{\text{CH}} \) order parameter values were then compared with the corresponding solid-state 2H-NMR-derived \( S_{\text{CD}} \) values. Both the \( S_{\text{CH}} \) and \( S_{\text{CD}} \) order parameters were consistent for those segmental positions having well-defined 13C chemical-shift assignments. However, in the region between 29.5 ppm and 31.5 ppm, we observed a discrepancy between the \( S_{\text{CH}} \) and \( S_{\text{CD}} \) order parameters for the DMPC bilayer at 30°C (Figs. S5 and S6). The discrepancies are more pronounced in the case of POPC lipid bilayers, where overlapping resonances from the palmitoyl and oleoyl hydrocarbon chains further complicate the peak assignments.

**Chemical-shift assignments of MAS carbon-13 NMR spectra**

With MAS, the 13C chemical shifts of lipid bilayers are not averaged to liquid-phase isotopic chemical shifts. Instead, they correspond to the chemical-shift values averaged over the molecular conformations present in the liquid-crystalline phase. By contrast, the NMR chemical shifts for a particular site \( i \) in the solution state \( \delta_{\text{iso}}(i) \) are averaged over all possible conformations because of the rapid molecular rotations and rotational isomerizations about the chemical bonds. Similar observations in proteins and polypeptides indicate that the 13C chemical shifts strongly depend on the average molecular conformation (88). The observed chemical shifts \( \delta_{\text{obs}}(i) \) under MAS can be expressed for a given segment position as \( \delta_{\text{obs}}(i) = \delta_{\text{iso}}^{(i)} + \Delta\delta^{(i)} \). The secondary chemical-shift values \( \Delta\delta^{(i)} \) are indicative of the molecular structures. For polymers, proteins, and polypeptides, a statistical analysis of \( \Delta\delta^{(i)} \) values provides an intrinsic probe for conformational characterization and secondary structure determination (88–90). An in-depth analysis of conformation-dependent chemical shifts in the case presented here requires theoretical calculations based on molecular orbital theory (91,92), which is beyond the scope of this work. One strategy for assigning the isotropic 13C
NMR chemical shifts entails selective $^2\text{H}$ isotopic labeling, leading to suppression of cross-polarization from the abundant $^1\text{H}$ nuclei (45). An alternative entails comparison of the dipolar order parameters to the quadrupolar order parameters measured in $^2\text{H}$ NMR spectroscopy, which we propose as a means of $|S_{\text{CD}}|$-assisted $^{13}\text{C}$ NMR spectral assignments.

In this work, we implemented the $|S_{\text{CD}}|$-assisted $^{13}\text{C}$ resonance assignments (see Figs. S6–S8) by making use of available $^2\text{H}$ solid-state NMR data (43). The resulting $|S_{\text{CH}}|$ order profiles as a function of carbon position are shown in Fig. 3 for DMPC, POPC, and EYSM bilayers in the liquid-crystalline (also known as the liquid-disordered (l_d)) state. The absolute order profiles show a decreasing trend as the peak (carbon) index $i$ changes from the headgroup to the acyl chain methyl end. Tethering of the acyl chains to the aqueous interface results in order parameters that are higher near the headgroups than near the methyl ends of the acyl chain (93). In the case of $^{13}\text{C}$ NMR for DMPC and EYSM (Fig. 3, a and d), the order parameters for the individual acyl chains were not separately identified. However, $^{13}\text{C}$ NMR for POPC (Fig. 3, b and c) shows that the unsaturated carbons (C9 and C10) and allylic carbons (C8 and C11), as well as additional carbon positions from the sn-2 acyl chain, were distinct from the sn-1 chain $^{13}\text{C}$ resonances. It follows that separate order profiles were determined for the palmitoyl and oleoyl chains (Fig. 3, b and c). Comparison of the dipolar $|S_{\text{CH}}|$ order parameters to the quadrupolar $|S_{\text{CD}}|$ order parameters is given in Figs. S7 and S8 for POPC in the l_d phase. For EYSM, assignments of the chemical shifts to the sphingosine backbone carbon positions were limited to the C1, C3, C4, and C5 sites. The C2 position was not observed, due either to line broadening caused by quadrupolar coupling to the $^{14}\text{N}$ nucleus or to its close chemical-shift proximity to the intense $\gamma$ choline methyl position.

The above findings show that solid-state $^{13}\text{C}$ NMR at natural abundance is complementary to $^2\text{H}$ NMR spectroscopy of membrane lipid bilayers (50). Bilayer structural properties including the volumetric hydrocarbon thickness and area per lipid can be obtained without the need for $^2\text{H}$-labeling, which can be time-consuming, expensive, and otherwise prohibitive (see below). The $^{13}\text{C}$ chemical-shift assignments, together with the dipolar couplings and segmental order parameters, are summarized in Tables S1–S5. Fig. 4 shows a comparison between the DROSS-derived $|S_{\text{CH}}|$ and $|S_{\text{CD}}|$ values for DMPC. For the DMPC bilayer at 50°C, in the liquid-crystalline (l_d) state, the nearly unit slope for the plot of $|S_{\text{CD}}|$ versus $|S_{\text{CH}}|$ (Fig. 4, a and b) indicates the consistence of both the $^2\text{H}$ solid-state NMR and $^{13}\text{C}$ SLF NMR results in calculating the lipid segmental order parameters. The $|S_{\text{CD}}|$-assisted assignments of the solid-state $^{13}\text{C}$ NMR chemical shifts lead to dipolar $|S_{\text{CH}}|$ order parameters that are generally in good agreement with the results of corresponding $^2\text{H}$ NMR experiments (35). However, the dynamic timescales that average out these interactions are dissimilar, owing to the difference between the rigid-lattice coupling constants (40.7 kHz for $^{13}\text{C}$ nuclei and 167 kHz for $^2\text{H}$ nuclei) (60,94). For DMPC at 30°C and for POPC, there are some additional deviations that could be due either to misassignment of some of the peaks or to different motional scalings of the lineshapes that may require future investigation (Figs. S5, S7, and S8).

**Cholesterol-containing lipid bilayers in the l_d phase**

One striking feature we consider in this work is the drastic increase of absolute order parameters for acyl chain segments of liquid-ordered (l_o) bilayers containing cholesterol versus l_d bilayers (95). Here, it is possible that the cholesterol may exert its effects through either the chains, the headgroup, or possibly both regions of the lipids. To better
understand the structural perturbations indicated by the RDCs, we performed DROSS experiments on POPC and EYSM bilayers in the $l_0$ phase containing 50 mol % cholesterol. Using the INEPT polarization transfer for liquid-crystalline samples, chemically shifted resonances are prominent for the distal alkyl chain positions because of the effective magnetization transfer. For relatively immobile molecular regions with large static dipolar couplings, several sterol ring positions are detected by Hartmann-Hahn cross-polarization techniques (96,97) that helped in assigning many positions of the sterol ring and alkyl chain chemical shifts of cholesterol (54). In general, the RDC line-shape quality is limited by the signal/noise ratio afforded by the chemically shifted resonances.

Representative order-parameter profiles showing the influence of cholesterol for the $l_0$ phases of POPC and EYSM are provided in Fig. 5. The higher magnitudes of $|S_{CH}|$ values for both lipid bilayers at various carbon positions are an indication of the $l_0$ phase (8,98–101) due to interaction with cholesterol (95,102,103). The nonequivalence of the segments of the sn-1 and sn-2 chains observed in $^2$H solid-state NMR experiments (104) is clearly reflected in the case of POPC (Fig. 5, a and b). There is a decreasing trend in $|S_{CH}|$ from the upper acyl positions toward the distal end of the chain. At the uppermost acyl sites (C2 segment of oleoyl and palmitoyl chains), an initial downturn effect corresponds to RDCs that are reduced compared with nearest-neighbor carbon positions. In addition, monounsaturation of the oleoyl chain at the C9 and C10 sites renders the two vinyl $^{13}$C-$^1$H positions orientationally nonequivalent both to each other and to the other saturated chain segments (104). The terminal methyl groups of the acyl chains exhibit a very small RDC because of the reorientation and threefold symmetry of the methyl $^{13}$C-$^1$H bonds. For EYSM, most notable are the $|S_{CH}|$ values associated with the sphingosine backbone sites (Fig. 5, c and d). The largest couplings of these sites are observed at the upper C3 position, which may participate in interfacial exchange-type C3-OH hydrogen bonding and/or in C3-OH acceptor and NH donor hydrogen bonding. The large value is suggestive of a static backbone orientation assisted by hydrogen-bonding in the $l_0$ phase and stabilized through lipid packing.

**DISCUSSION**

Separated local-field spectroscopy (45–47) at natural $^{13}$C abundance expands the range of applications of solid-state NMR in membrane biophysics in significant new ways. The development and use of biophysical methods for
biomembranes can benefit by extending the $^2$H NMR approach (50) to cases where $^3$H-isotope labeling is impractical. Sphingolipids and other natural lipids can be investigated, together with their interactions both with cholesterol and in raftlike lipid mixtures and with membrane proteins. It has been proposed that in complexes with cholesterol and/or receptor proteins, sphingolipids form functional microdomains in putative lipid rafts (9,19,105,106). Such membrane lipids in the brain and other organs are associated with second-messenger events implicated in intracellular signaling and cholesterol shuttling (23,107,108). Applications of solid-state $^{13}$C NMR methods to polyunsaturated lipid bilayers (72,109) have also been described. In these examples and others, we are interested in the relationship between molecular properties of membrane lipids and their biological functions within the broader context of structural biophysics (1,5,6,11).

$^{13}$C-$^1$H dipolar couplings allow calculations of lipid bilayer structure

The DROSS experimental method (46) allows measurement of the direct $^{13}$C-$^1$H dipolar couplings in liquid-crystalline systems, such as lipid bilayers at natural isotopic abundance. Through-space direct $^{13}$C-$^1$H dipolar interactions report on the orientation of the individual $^{13}$C-$^1$H bonds with respect to the bilayer normal, and they are mathematically isomorphic to the C-$^1$H bond order parameters measured by $^2$H solid-state NMR spectroscopy. Moreover, unlike $^2$H solid-state NMR, this technique makes it possible to obtain the average orientation of C-H bond segments without isotopic labeling. Analogous studies have also been performed using switched-angle spinning and off-MAS experiments (110). However, DROSS has multiple advantages over the other experiments mentioned here. For instance, implementation of DROSS does not require specialized hardware to control the orientation of the rotor during the experiment. Another advantage is the ability of DROSS to define the sign of the dipolar coupling with a single set of scaling factors (46). The experiment takes advantage of the larger chemical-shift dispersion of the $^{13}$C nucleus that enables assignment to be made to specific carbon atoms. Despite these advantages, however, the DROSS experiment for lipid membranes suffers from significant $^{13}$C signal superposition, thus limiting the precision of peak assignments and measurement of assigned order parameters. On the other hand, $\omega-3$ polyunsaturated lipid acyl groups show better resolution of $^{13}$C chemical shifts (111), so that DROSS can be conveniently applied as shown by Gawrisch and co-workers (47).

Dipolar order parameters reflect structural and dynamic features of phospholipids and sphingolipids

These studies aim at determining the membrane structural parameters using the largest absolute order parameter as typical of the lipid segments near the headgroup. Because DROSS can determine these order parameters unambiguously, it is a suitable technique for such structural studies. The DROSS experiment enables the order parameters to be assigned to specific carbon atoms in the $I_d$ phase at natural isotopic abundance (see Fig. 1). In the case of the disaturated lipid DMPC, there is significant overlap of $^{13}$C resonances from the middle of the hydrocarbon chain, yet we could resolve four to five peaks for eight of the carbons (C4—C11). Detailed assignments are not available for this crowded spectral region. First, we assigned these peaks by calculating the chemical shifts using the additivity rules proposed for isotropic liquids (61–65). With such assignments, the measured $|S_{CH}|$ order parameters for DMPC lipids agreed well with solid-state $^2$H-NMR-determined $|S_{CD}|$ values (43,112). The overlapped methylene carbon resonances around 30.5 ppm are also incompletely resolved in $^2$H NMR, and lead to a plateau region in the order profile. A similar assignment strategy did not work for POPC, as the signals from saturated and unsaturated acyl chains significantly overlap. However, by comparing the absolute $|S_{CH}|$ order parameters with $^2$H-NMR-derived $|S_{CD}|$ order parameters, we could identify the carbon chemical-shift positions. For POPC, the carbon resonances of the unsaturated region (C9 and C10) and the immediately adjacent allylic carbons (C8 and C11) were clearly identified. The order parameter values for the unambiguously identified carbon positions of the palmitoyl and oleoyl chains were consistent with the corresponding $|S_{CD}|$ values. The lower order parameter values for the unsaturated carbon positions compare favorably with those from $^2$H NMR and MD simulations (93). Notably, EYSM showed higher order parameters than the other lipid bilayers studied, indicating its lower flexibility in the single-component bilayer. Complete peak assignments were not essential for the structural parameter calculations. Thus, the highest order parameter shown by the acyl segments, which corresponds to the plateau value of the $^2$H NMR order profile, was chosen for structural calculations.

The mean-torque model explains ordering of sphingolipids versus phospholipids

Next, we used dipolar $^{13}$C-$^1$H order parameters in combination with the mean-torque model (35) to determine the average cross-sectional area per lipid, $\langle A \rangle$, and volumetric hydrocarbon chain thickness, $D_{C_2}$, of the DMPC bilayer in the $I_d$ phase, and for POPC and EYSM in both the $I_d$ and $I_o$ phases. This structural model has previously been used successfully with $^2$H NMR order parameters (35,74,113). To avoid complications from chain upturns, the largest dipolar order parameters are used for solid-state $^{13}$C NMR; these values correspond to the plateau value used in treating the $^2$H NMR data. Comparison of the bilayer structural parameters from $^{13}$C NMR shows good agreement with the corresponding $^2$H NMR data (Fig. 4). Referring to
FIGURE 6 Bilayer structural parameters obtained from SLF $^{13}$C NMR spectroscopy agree with results from solid-state $^2$H NMR spectroscopy of lipids that have perdeuterated acyl groups. Parameter values obtained using $^2$H solid-state NMR are compared with those obtained using the SLF $^{13}$C NMR experiment DROSS for bilayer thickness, $D_h$ (squares), and area per lipid, $\langle A \rangle$ (circles). For DMPC and POPC bilayers, structural data are shown at temperatures of 30°C (solid circles) and 50°C (gray-filled circles), and at 28°C (squares) and 48°C (gray-filled squares), respectively. Cross-sectional lipid areas are calculated using the plateau $[S_{CD}]$ value in the case of $^2$H NMR and the highest $[S_{CD}]$ value of the acyl segments in the case of $^{13}$C NMR spectroscopy. The unit slope indicates excellent agreement of the two methods. Note that isotopic labeling is not required in the case of solid-state $^{13}$C NMR spectroscopy. The estimated error bars correspond to the standard deviations in the measured RDCs in multiple DROSS experiments. To see this figure in color, go online.

Table 1 Structural parameters for lipid bilayers obtained from solid-state $^{13}$C and $^2$H NMR spectroscopy

<table>
<thead>
<tr>
<th>Lipid</th>
<th>$T$ (°C)</th>
<th>$D_{lc}$ ($^1$H)</th>
<th>$D_{bc}$ ($^2$H)</th>
<th>$\langle A \rangle$ ($^1$H)</th>
<th>$\langle A \rangle$ ($^2$H)</th>
</tr>
</thead>
<tbody>
<tr>
<td>DMPC</td>
<td>30</td>
<td>12.9 ± 0.5</td>
<td>12.8 ± 0.3</td>
<td>43.8 ± 2.6</td>
<td>43.6 ± 0.9</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>11.4 ± 0.4</td>
<td>11.9 ± 0.2</td>
<td>41.6 ± 2.5</td>
<td>41.8 ± 0.8</td>
</tr>
<tr>
<td>POPC</td>
<td>28</td>
<td>14.8 ± 0.6b</td>
<td>13.6 ± 0.3b</td>
<td>51.8 ± 3.1</td>
<td>52.4 ± 1.1</td>
</tr>
<tr>
<td></td>
<td>48</td>
<td>16.7 ± 0.7</td>
<td>15.3 ± 0.4</td>
<td>46.6 ± 2.8</td>
<td>50.2 ± 1.0</td>
</tr>
<tr>
<td>EYSM</td>
<td>48</td>
<td>12.8 ± 0.5b</td>
<td>14.2 ± 0.3b</td>
<td>51.0 ± 3.1</td>
<td>48.8 ± 1.0</td>
</tr>
<tr>
<td>POPC/Cholesterol (1:1)</td>
<td>48</td>
<td>14.4 ± 0.6b</td>
<td>16.0 ± 0.3b</td>
<td>51.5 ± 2.1</td>
<td>54.9 ± 1.1</td>
</tr>
<tr>
<td></td>
<td>19.4 ± 0.8</td>
<td>—</td>
<td>—</td>
<td>45.1 ± 0.9</td>
<td>—</td>
</tr>
<tr>
<td>EYSM/Cholesterol (1:1)</td>
<td>48</td>
<td>17.5 ± 0.7</td>
<td>18.0 ± 0.7</td>
<td>53.5 ± 3.2</td>
<td>45.5 ± 2.7</td>
</tr>
</tbody>
</table>

*Error bars correspond to the standard deviations propagated from multiple experimental measurements of RDCs.
$^b$sn-1 hydrocarbon chain.
$^c$sn-2 hydrocarbon chain.

Configurational entropy governs mixing of sphingolipids and phospholipids with cholesterol

Solid-state $^2$H NMR spectroscopy (85,115) has previously established an umbrella-like model for cholesterol-phospholipid interactions, where the cholesterol C3-OH group is situated beneath the phospholipid headgroups, so that it acts as a spacer molecule as originally proposed by Brown and Seelig (85). Thermodynamically, the cholesterol interactions with DMPC, POPC, and/or EYSM membranes are driven by the hydrophobic effect plus van der Waals interactions between the acyl chains and sterol ring system, giving an I$_l$ phase beyond a threshold cholesterol concentration (116–118). Cholesterol is found to significantly increase...
the hydrocarbon thickness of the POPC bilayer. Such large volumetric thicknesses are characteristic of both the POPC and EYSM l\textsubscript{o} phases. The average bilayer thicknesses for cholesterol-enriched l\textsubscript{o} phases are \( D_{h0} \approx 56.8 \text{ Å} \) and 50.0 Å for POPC and EYSM, respectively. The average cross-sectional areas in the l\textsubscript{o} phase are reduced owing to the condensing effect of cholesterol, as discussed by McConnell and co-workers (119). For bilayers containing cholesterol (1:1) we find that \( \langle A \rangle = 45.1 \text{ Å}^2 \), and for EYSM, \( \langle A \rangle = 45.5 \text{ Å}^2 \) at 48°C (Table 1). The cholesterol ordering effect on lipid bilayer stiffening is limited by the maximum acyl length. Furthermore, membranes comprising EYSM/cholesterol may be affected by sphingosine backbone hydrogen bonding and packing interfacial hydrogen bonding involving the NH donor and cholesterol C3-OH acceptor. Such interactions are observed in MD simulations (120,121), although supporting experimental evidence remains elusive (122–127). Another observation is that the sphingosine backbone possesses both an OH hydrogen-bond acceptor and an NH hydrogen-bond donor, which may lead to interlipid hydrogen-bonding and possibly to super-lattice formation in the l\textsubscript{o} phase (128).

Readers should note that the cholesterol-mediated structural perturbations are clearly less pronounced for the sphingolipid EYSM than for POPC in the l\textsubscript{o} phase. Upon addition of 50 wt % cholesterol, the increase in absolute segmental order parameters is \( \approx 0.25 \) for POPC and \( \approx 0.12 \) for EYSM, as indicated in Fig. 5, b and c (comparisons are for the maximum \( \delta_{\text{CH}} \) values due to the plateau region of the order profiles). Correspondingly, the increase in the hydrocarbon thickness and condensation of area per lipid is less for EYSM than for POPC bilayers. Such a remarkable difference indicates that EYSM is in a relatively ordered state in the single-component membrane. The higher acyl segmental order parameters in single-component bilayers at a given temperature for EYSM relative to POPC indicates the high propensity of self-association for the hydrophobic moieties of sphingomyelin lipids (9,27). Notably, these observations suggest that the entropic loss upon adding cholesterol is less pronounced for EYSM than for POPC. A greater loss of conformational entropy for POPC versus EYSM may explain selective enrichment of sphingomyelin in putative raftlike microdomains. Mixing of cholesterol is more favorable for sphingolipids compared to phosphatidylcholines, potentially driving the formation of lipid rafts in multicomponent biomembranes (129–131). That is to say, like dissolves like—as we learn in our introductory chemistry courses.

CONCLUSIONS

Natural-abundance \(^{13}\text{C}\) separated local-field NMR together with a mean-torque model gives lipid structural parameters that are complementary to those from solid-state \(^{2}\text{H}\) NMR spectroscopy. The \(^{13}\text{C}^{-}{^{1}}\text{H}\) residual dipolar couplings of membrane lipids were successfully used to calculate the area per lipid and bilayer thickness. Differences in molecular interactions are resolved by site-specific \(^{13}\text{C}\) chemical shifts and \( \delta_{\text{CH}} \) dipolar order parameters, giving insight into interfacial molecular packing and hydrophobic interactions. The behavior of glycerophospholipids and sphingolipids in the l\textsubscript{o} and l\textsubscript{d} phases reflects the balance of compositional heterogeneity and chemical structure in biological systems. Despite a common thermodynamic l\textsubscript{d} phase for both lipids, their molecular interactions with cholesterol vary significantly. The higher order of EYSM lipids versus POPC lipids implies that the entropy loss due to interactions with cholesterol is less, favoring the association of EYSM over POPC in raftlike lipid mixtures. Moreover, SLF NMR experiments can address key membrane lipid roles of polyunsaturated lipid bilayers and lipid mixtures containing biologically active peptides or proteins. An important question for future research is how the average material properties emerge from the atomic-level interactions in lipid bilayers as investigated by solid-state NMR spectroscopy and related biophysical methods.

SUPPORTING MATERIAL

Eight figures, five tables, and supporting methods are available at http://www.biophysj.org/biophysj/supplemental/S0006-3495(14)00789-9.

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SUPPORTING CITATIONS

Reference (132) appears in the Supporting Material.

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